

Name: \_\_\_\_\_

Course/Section: \_\_\_\_\_

Instructor: \_\_\_\_\_

## Chapter 7 Radical Expressions and Functions

### 7.1 Radical Expressions and Functions

Radical Notation ~ The Square Root Function ~ The Cube Root Function

#### STUDY PLAN

**Read:** Read Section 7.1 on pages 492-500 in your textbook or eText.

**Practice:** Do your assigned exercises in your  Book  MyMathLab  Worksheets

**Review:** Keep your corrected assignments in an organized notebook and use them to review for the test.

#### Key Terms

*Exercises 1-8: Use the vocabulary terms listed below to complete each statement.*

*Note that some terms or expressions may not be used.*

**radicand**

**cube root**

**radical sign**

**odd root**

**radical expression**

**$n$ th root**

**index**

**even root**

**square root**

**principal  $n$ th root**

1. The symbol  $\sqrt{\quad}$  is called the \_\_\_\_\_.
2. The \_\_\_\_\_ function is given by  $f(x) = \sqrt[3]{x}$ .
3. If  $a > 0$  and  $n$  is even, then the positive  $n$ th root is denoted  $\sqrt[n]{a}$  and is called the \_\_\_\_\_ of  $a$ .
4. An expression containing a radical sign is called a(n) \_\_\_\_\_.
5. The \_\_\_\_\_ function is given by  $f(x) = \sqrt{x}$ .
6. The number  $b$  is a(n) \_\_\_\_\_ of  $a$  if  $b^n = a$ .
7. The equation  $\sqrt[n]{a} = b$  means that  $b^n = a$ , where  $n$  is a natural number called the \_\_\_\_\_. If  $n$  is odd, we are finding a(n) \_\_\_\_\_ and if  $n$  is even, we are finding a(n) \_\_\_\_\_.
8. The expression under the radical sign is called the \_\_\_\_\_.

**Radical Notation**

*Exercises 1-19: Refer to Examples 1-7 on pages 492-496 in your text and the Section 7.1 lecture video.*

1. Find the square roots of 144. 1. \_\_\_\_\_

*Evaluate each square root.*

2.  $\sqrt{64}$  2. \_\_\_\_\_

3.  $\sqrt{0.36}$  3. \_\_\_\_\_

4.  $\sqrt{\frac{16}{25}}$  4. \_\_\_\_\_

5.  $\sqrt{d^2}$ ,  $d < 0$  5. \_\_\_\_\_

6. Approximate  $\sqrt{19}$  to the nearest thousandth. 6. \_\_\_\_\_

7. A formula for calculating the distance  $d$  in miles that one can see to the horizon on a clear day is approximated by  $d = 1.22\sqrt{x}$ , where  $x$  is the elevation, in feet, of person.

(a) Approximate how far a 5.75-foot-tall person can see to the horizon. 7.(a) \_\_\_\_\_

(b) Approximate how far a person can see from a 9500-foot mountain. (b) \_\_\_\_\_

*Evaluate the cube root. Approximate your answer to the nearest hundredth when appropriate.*

8.  $\sqrt[3]{27}$  8. \_\_\_\_\_

9.  $\sqrt[3]{-64}$  9. \_\_\_\_\_

10.  $\sqrt[3]{\frac{1}{8}}$  10. \_\_\_\_\_

11.  $\sqrt[3]{a^{12}}$  11. \_\_\_\_\_

12.  $\sqrt[3]{12}$  12. \_\_\_\_\_

*Evaluate each root, if possible.*

13.  $\sqrt[4]{625}$  13. \_\_\_\_\_

14.  $\sqrt[5]{-243}$  14. \_\_\_\_\_

15.  $\sqrt[4]{-16}$  15. \_\_\_\_\_

16.  $-\sqrt[4]{16}$  16. \_\_\_\_\_

Write each expression in terms of an absolute value.

17.  $\sqrt{z^2}$  17. \_\_\_\_\_

18.  $\sqrt{(x-2)^2}$  18. \_\_\_\_\_

19.  $\sqrt{x^2 + 6x + 9}$  19. \_\_\_\_\_

### The Square Root Function

*Exercises 20-26: Refer to Examples 8-12 on pages 496-499 in your text and the Section 7.1 lecture video.*

If possible, evaluate  $f(1)$  and  $f(-2)$  for each  $f(x)$ .

20.  $f(x) = \sqrt{4x-3}$  20. \_\_\_\_\_  
\_\_\_\_\_

21.  $f(x) = \sqrt{13-x^2}$  21. \_\_\_\_\_  
\_\_\_\_\_

22. If a football is kicked  $x$  feet high, then the time  $T$  in seconds that the ball is in the air is given by the function

$$T(x) = \frac{\sqrt{x}}{2}.$$

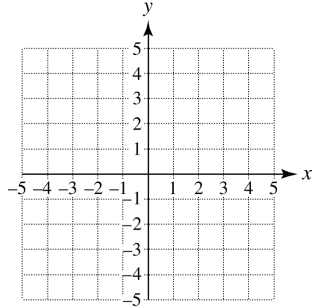
- (a) Find the hang time if the ball is kicked 30 feet into the air. 22.(a) \_\_\_\_\_

- (b) Does the hang time triple if the ball is kicked 90 feet into the air? (b) \_\_\_\_\_

23. Let  $f(x) = \sqrt{x-3}$ .

(a) Find the domain of  $f$ . Write your answer in interval notation. **23.(a)** \_\_\_\_\_

(b) Graph  $y = f(x)$  and compare it to the graph of  $y = \sqrt{x}$ . **(b)** \_\_\_\_\_



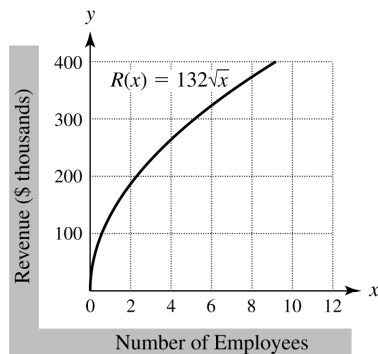
*Find the domain of each function. Write your answer in interval notation.*

24.  $g(x) = \sqrt{2x+4}$  **15.** \_\_\_\_\_

25.  $f(x) = \sqrt{x^2+3}$  **16.** \_\_\_\_\_

26. The function  $R(x) = 132\sqrt{x}$  gives the total revenue per year in thousands of dollars generated by a small business having  $x$  employees. A graph of  $y = R(x)$  is shown in the figure.

Revenue as a Function of Employees



(a) Approximate values for  $R(4)$ ,  $R(8)$ , and  $R(12)$  by using both the formula and the graph. **26.(a)** \_\_\_\_\_

(b) Evaluate  $R(12) - R(8)$  and  $R(8) - R(4)$  using the formula. Interpret your answer. **(b)** \_\_\_\_\_

**The Cube Root Function**

*Exercises 27-28: Refer to Example 13 on page 500 in your text and the Section 7.1 lecture video.*

*Evaluate  $f(1)$  and  $f(-3)$  for each  $f(x)$ .*

27.  $f(x) = \sqrt[3]{2x^2 - 1}$

27. \_\_\_\_\_  
\_\_\_\_\_

28.  $f(x) = \sqrt[3]{9 - x^2}$

28. \_\_\_\_\_  
\_\_\_\_\_